

LECTURE 21

BST AND TREE TRAVERSALS

MCS 275 Spring 2022

Emily Dumas

LECTURE 21: BST AND TREE TRAVERSALS

Course bulletins:

- Worksheet 8 available.
- Project 2 grading underway.
- I know project 2 proved to be challenging for many students.
- Project 3 will be posted this week, is due Friday 18 March.

UPDATE BST CLASS

Let's make it so that `BST ()` is considered a valid, empty tree.

TREEUTIL

I added a module to the `trees` sample code folder which can generate random trees. You'll use it in lab this week.

- [Documentation of `treeutil` module](#)

INTEGERSET

As a sample application of BST, we can make a class that stores a set of integers, supporting membership testing and adding new elements.

Compare alternatives:

- Unsorted list - fast to insert, but slow membership test
- Sorted list - fast membership test, slow insert

IMPLEMENTATION HIDING

To use `BST`, you need to know about and work with `Node` objects.

In contrast, `IntegerSet` has an interface based directly on the values to be stored. It hides the fact that its implementation uses a `BST`.

WALKING A TREE

Back to discussing binary trees (not necessarily BST).

For some purposes we need to visit every node in a tree and perform some action on them.

To do this is to **traverse** or **walk** the tree.

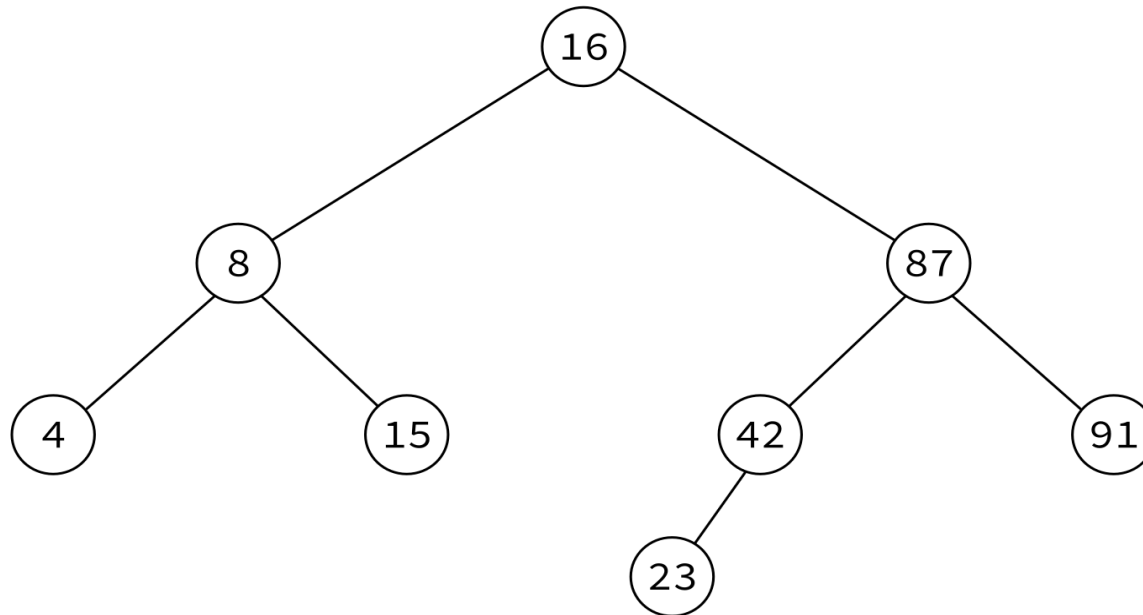
NAMED TRAVERSALS

The three most-often used recursive traversals:

- **preorder** - Node, left subtree, then right subtree.
- **postorder** - Left subtree, right subtree, then node.
- **inorder** - Left subtree, node, then right subtree.

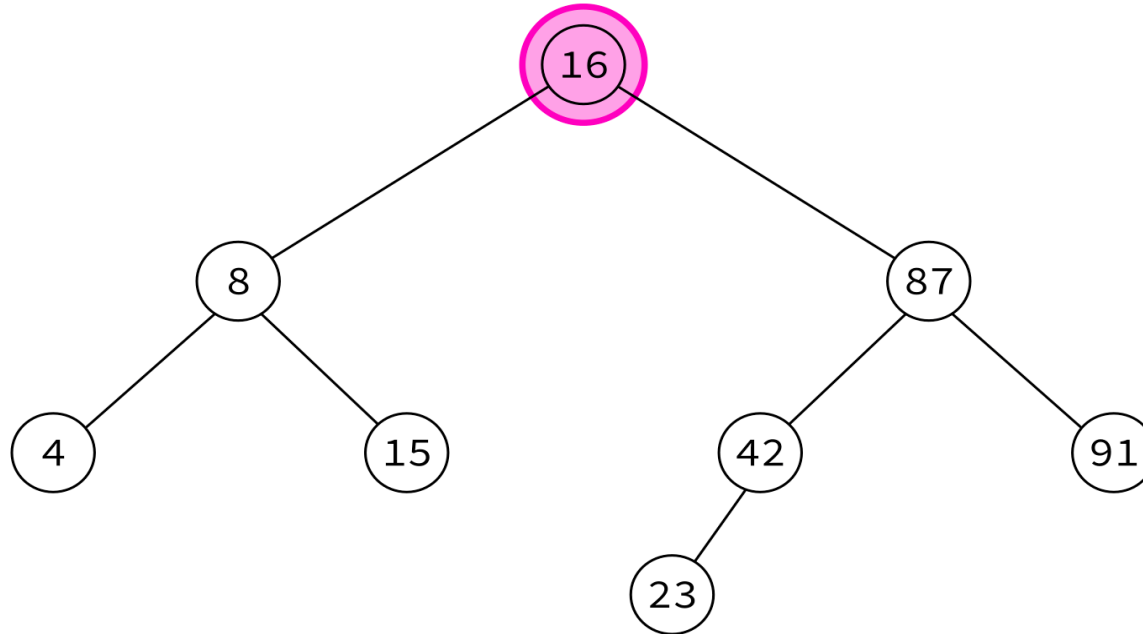
Note: They all visit left child before right child.

PREORDER TRAVERSAL



node, left, right

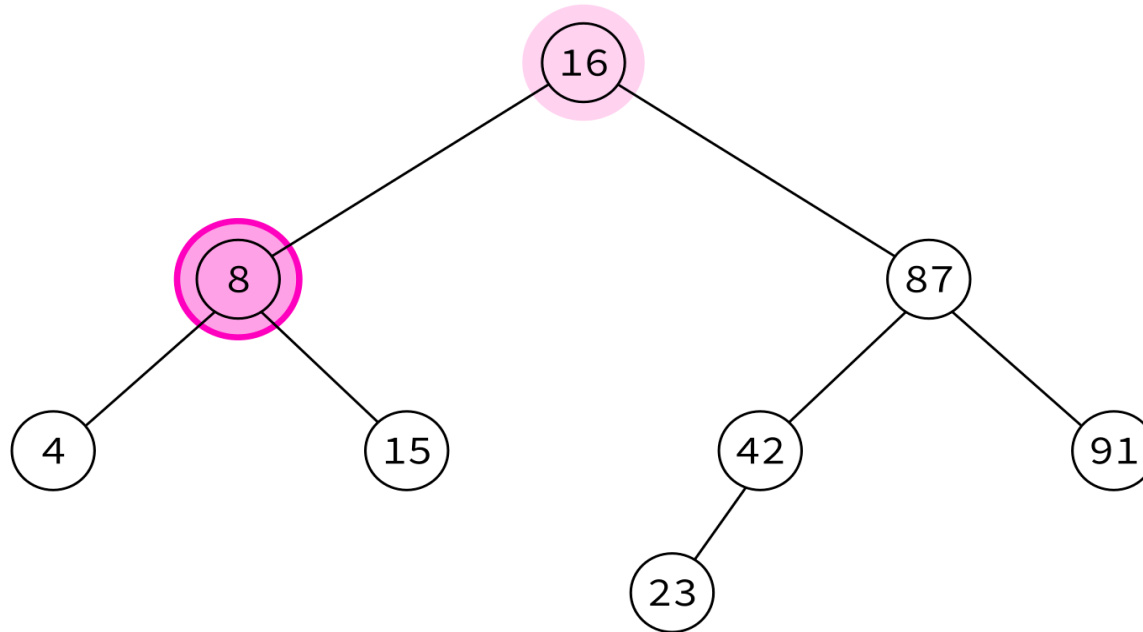
PREORDER TRAVERSAL



16,

node, left, right

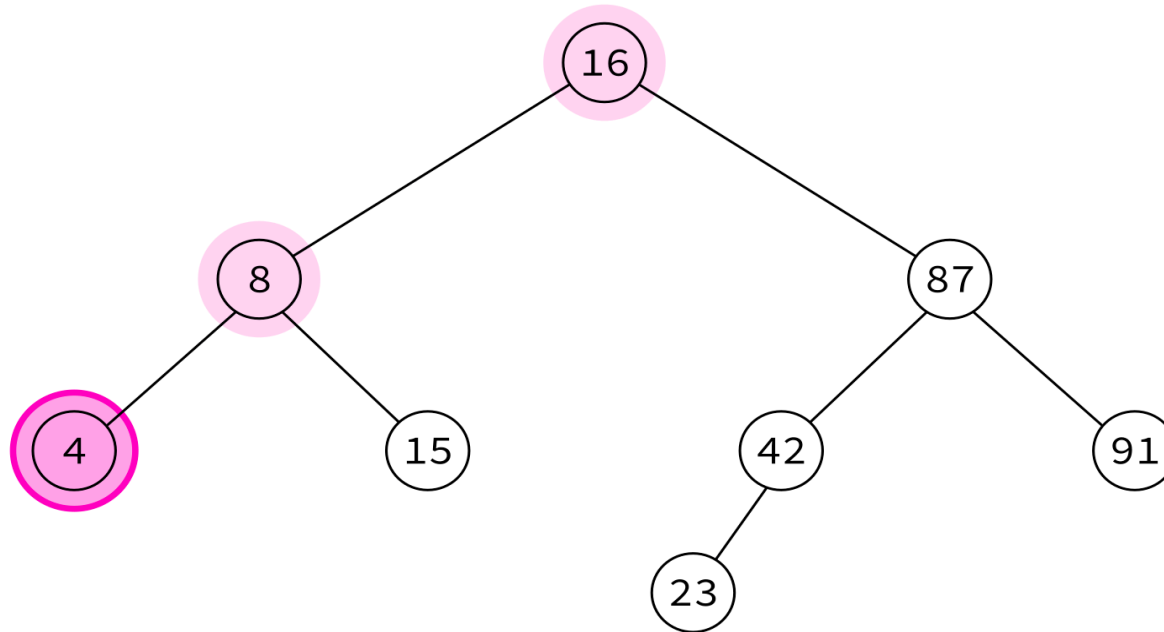
PREORDER TRAVERSAL



16, 8,

node, left, right

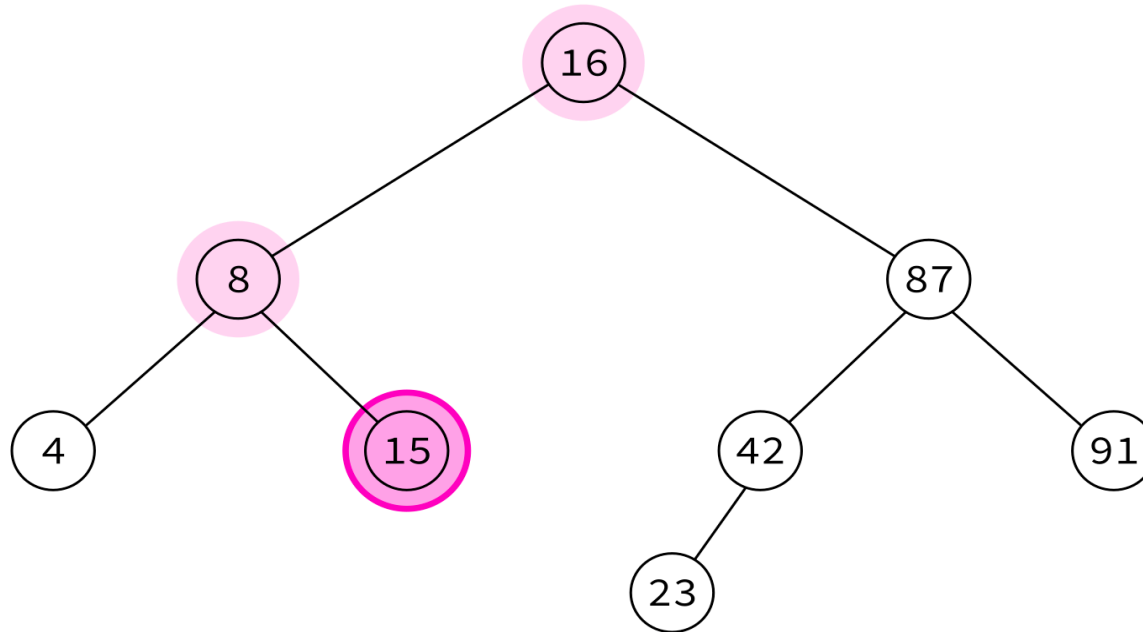
PREORDER TRAVERSAL



16, 8, 4,

node, left, right

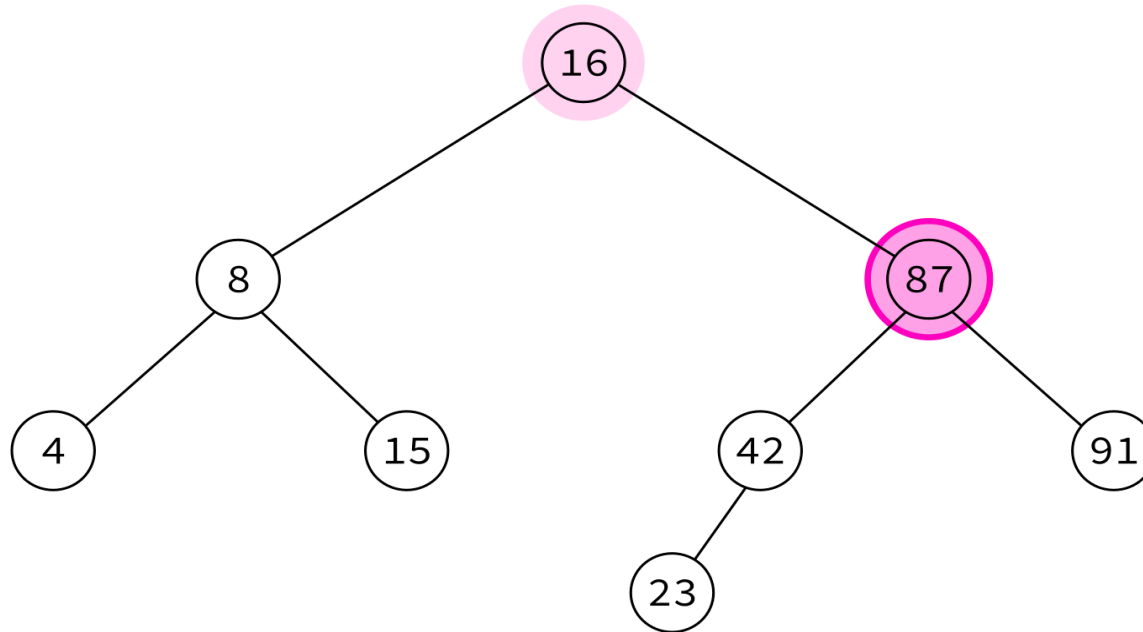
PREORDER TRAVERSAL



16, 8, 4, 15,

node, left, right

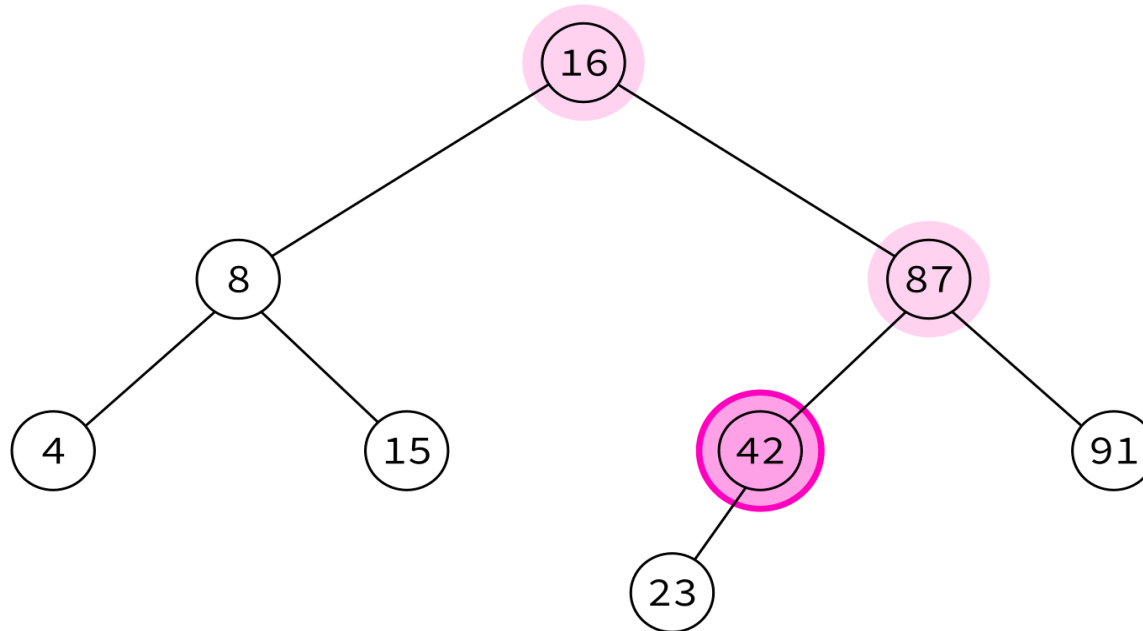
PREORDER TRAVERSAL



16, 8, 4, 15, 87,

node, left, right

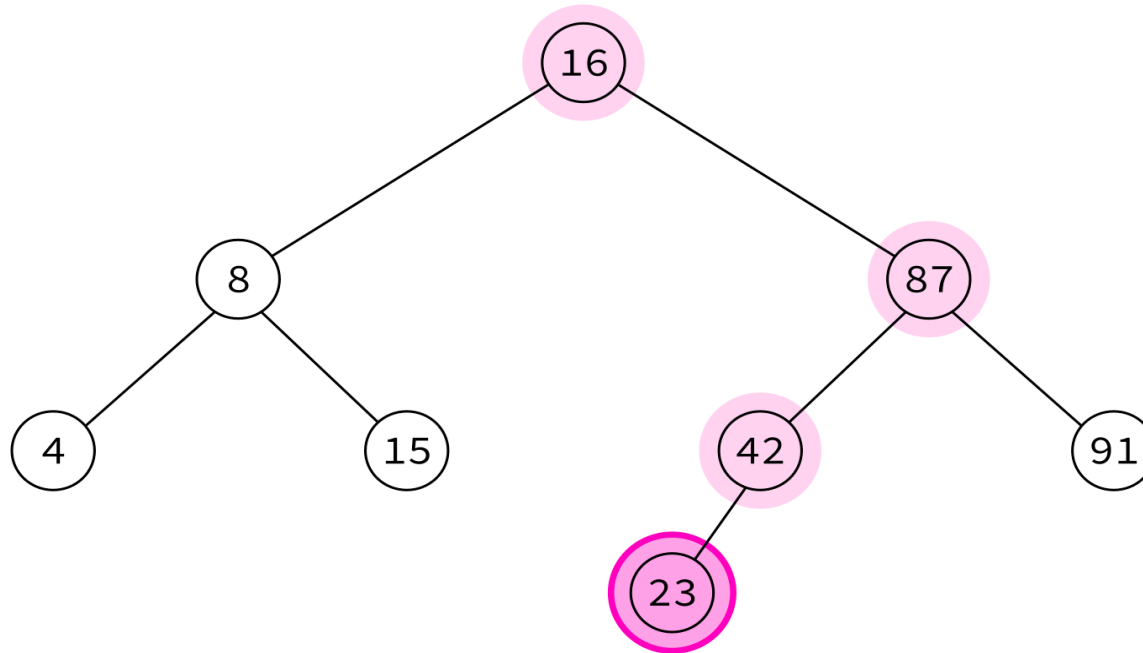
PREORDER TRAVERSAL



16, 8, 4, 15, 87, 42,

node, left, right

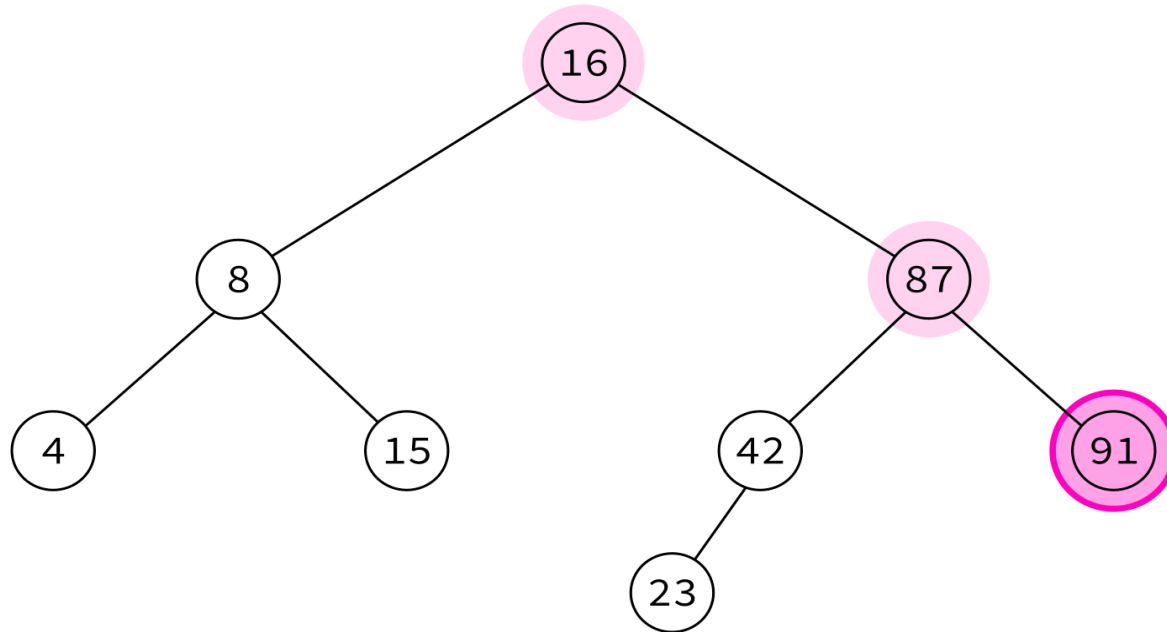
PREORDER TRAVERSAL



16, 8, 4, 15, 87, 42, 23,

node, left, right

PREORDER TRAVERSAL



16, 8, 4, 15, 87, 42, 23, 91

node, left, right

PREORDER TRAVERSAL

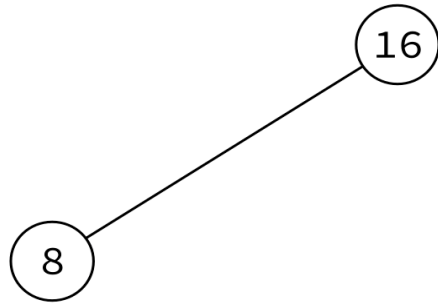
Typical use: Make a copy of the tree.

Insert the keys into an empty BST in this order to recreate the original tree.

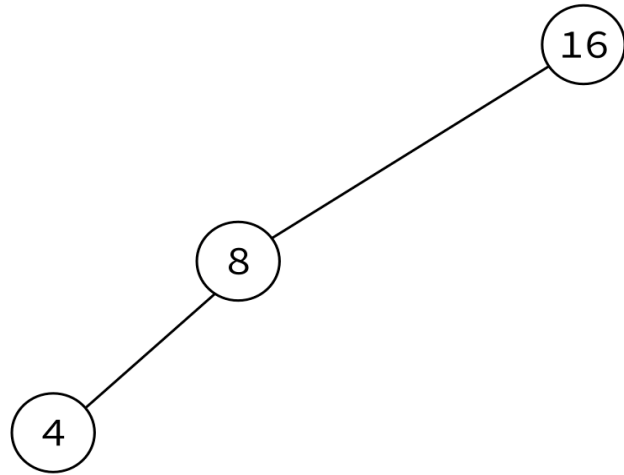
16, 8, 4, 15, 87, 42, 23, 91

16

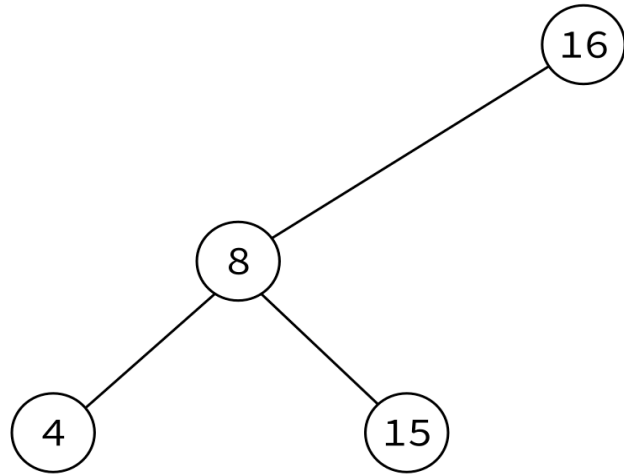
16, 8, 4, 15, 87, 42, 23, 91



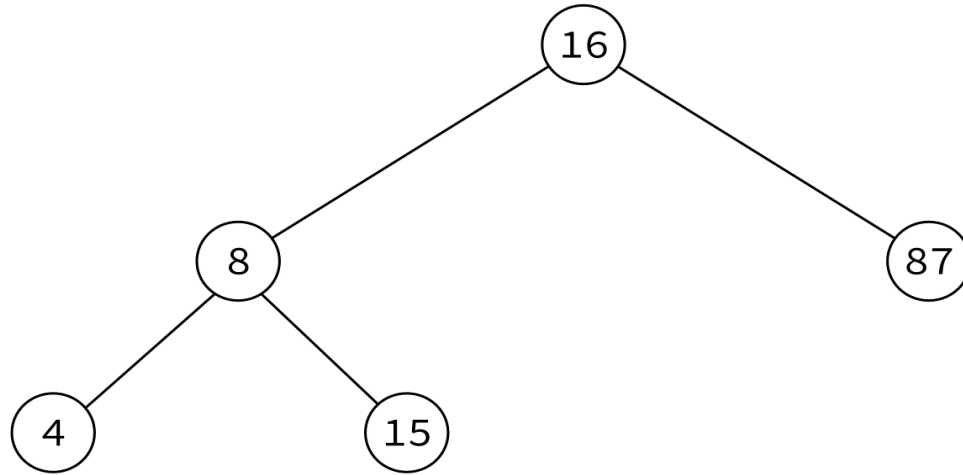
16, 8, 4, 15, 87, 42, 23, 91



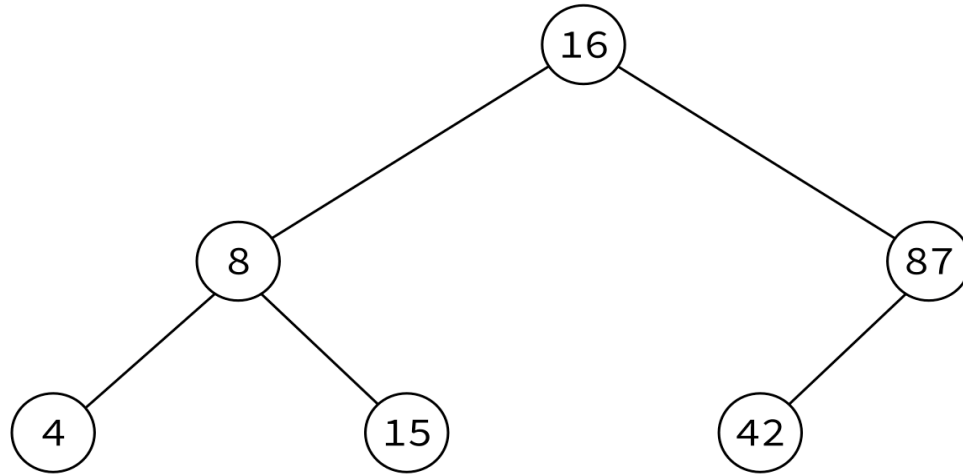
16, 8, 4, 15, 87, 42, 23, 91



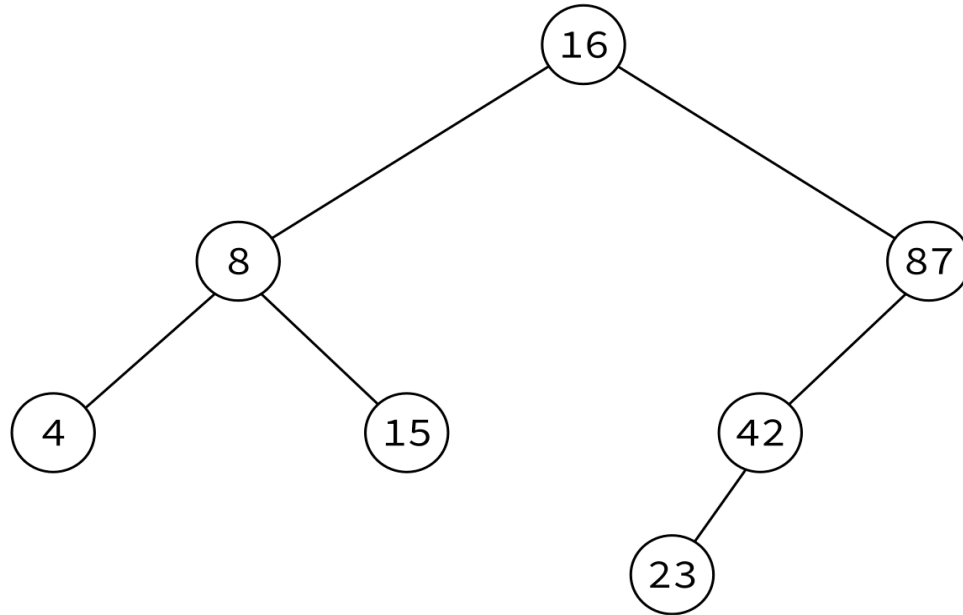
16, 8, 4, 15, 87, 42, 23, 91



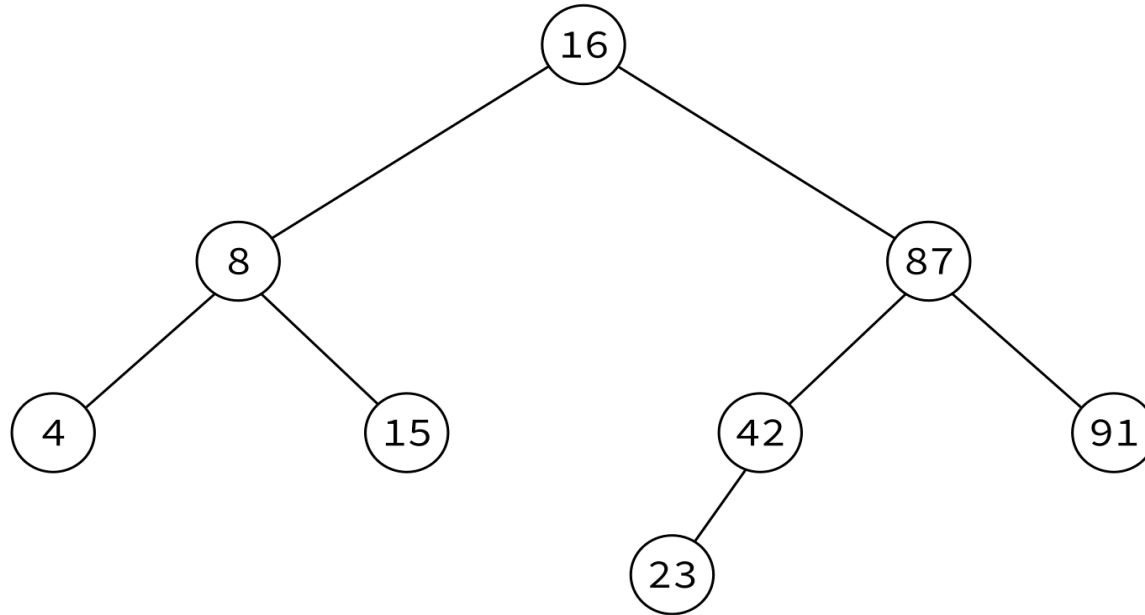
16, 8, 4, 15, 87, 42, 23, 91



16, 8, 4, 15, 87, 42, 23, 91

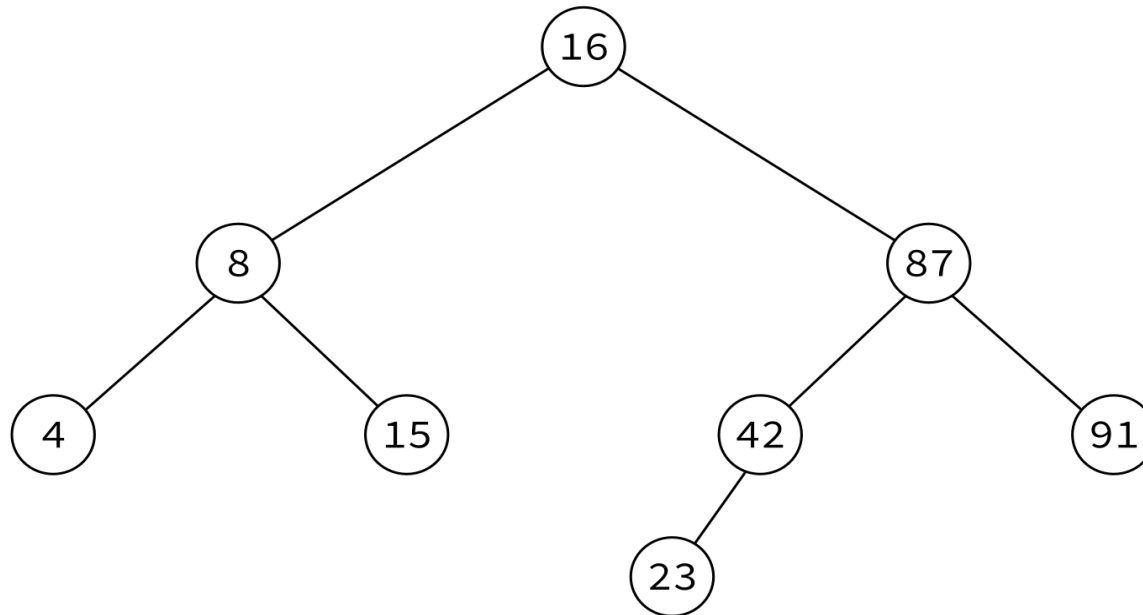


16, 8, 4, 15, 87, 42, 23, 91



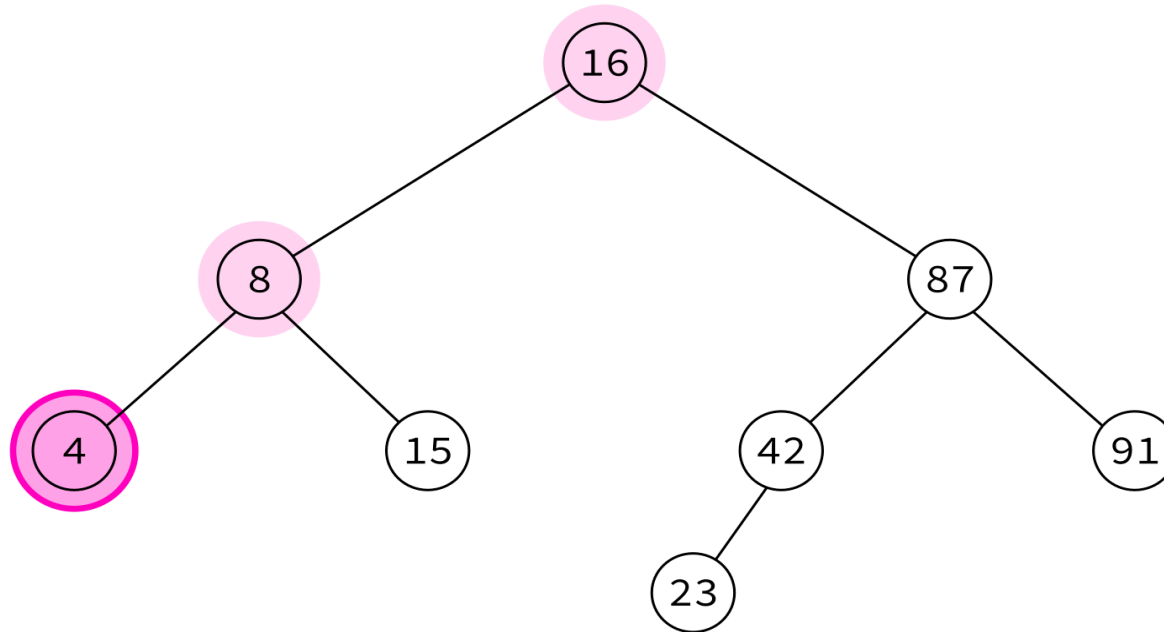
16, 8, 4, 15, 87, 42, 23, 91

POSTORDER TRAVERSAL



left, right, node

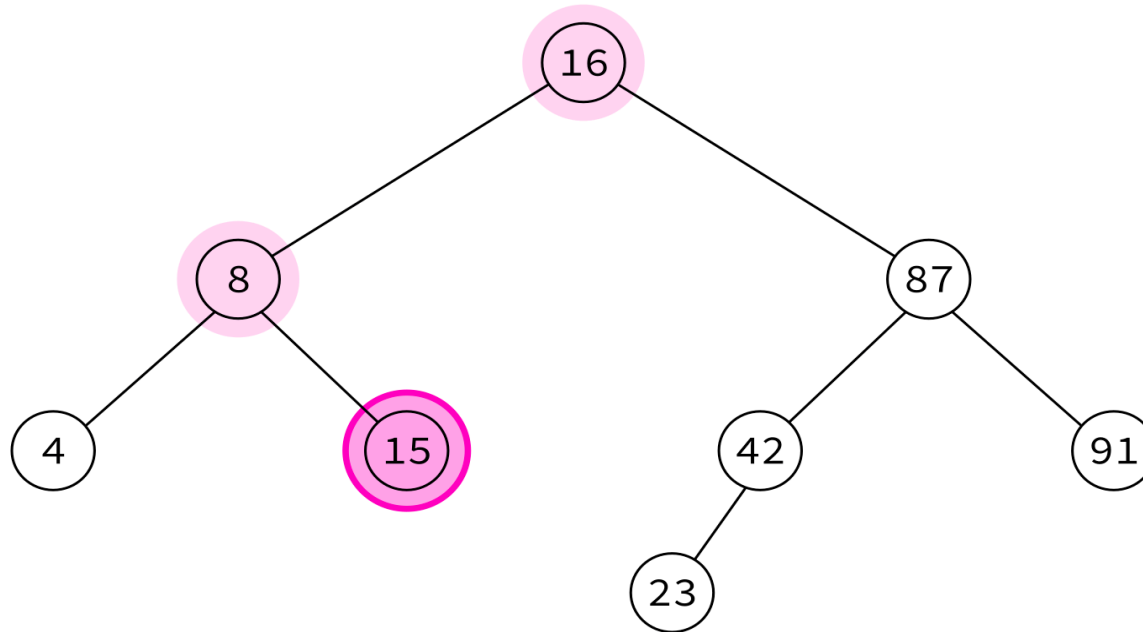
POSTORDER TRAVERSAL



4,

left, right, node

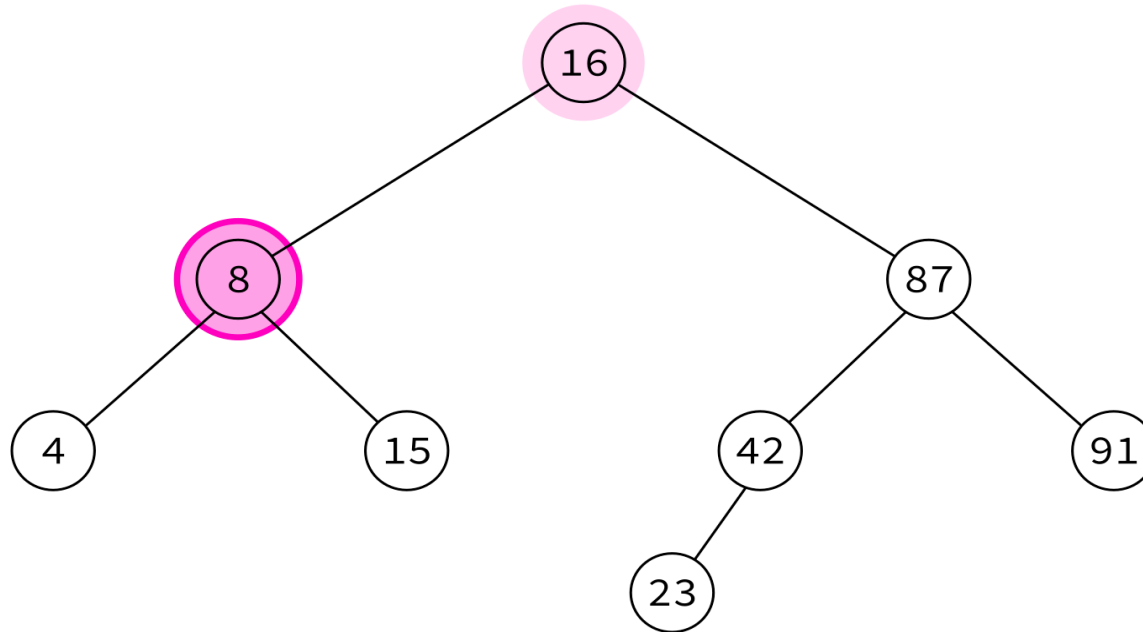
POSTORDER TRAVERSAL



4, 15,

left, right, node

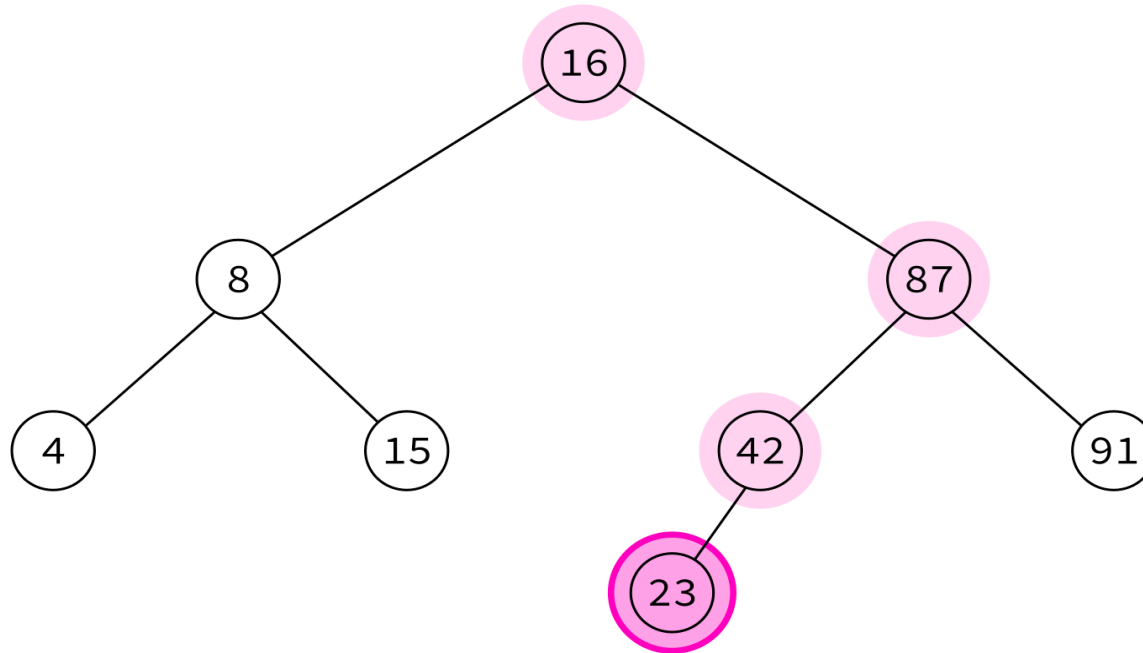
POSTORDER TRAVERSAL



4, 15, 8,

left, right, node

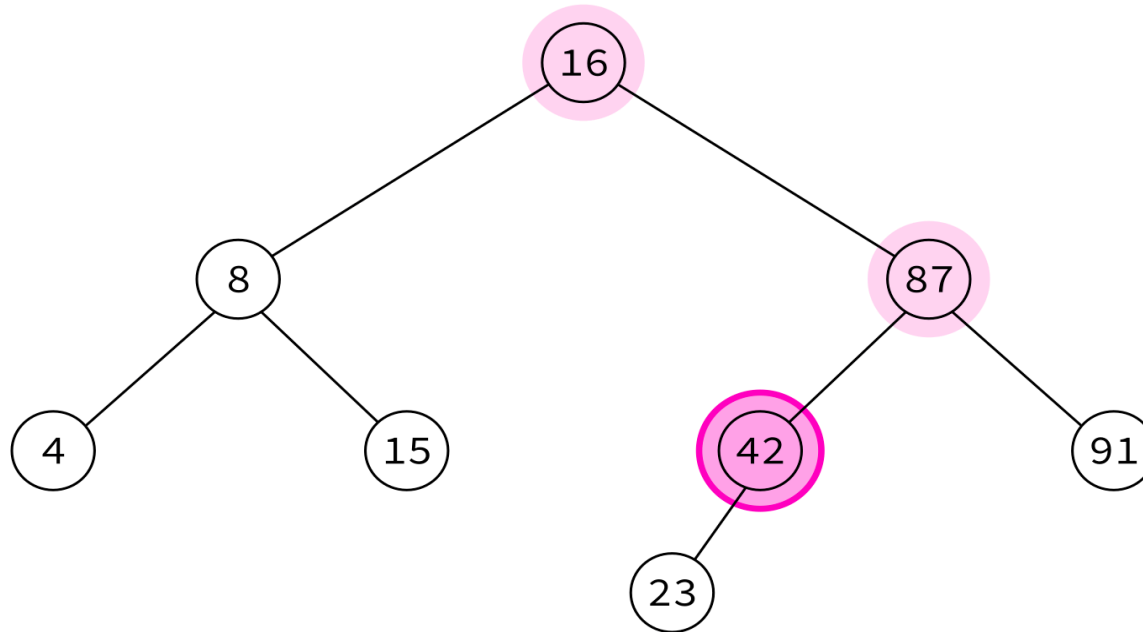
POSTORDER TRAVERSAL



4, 15, 8, 23,

left, right, node

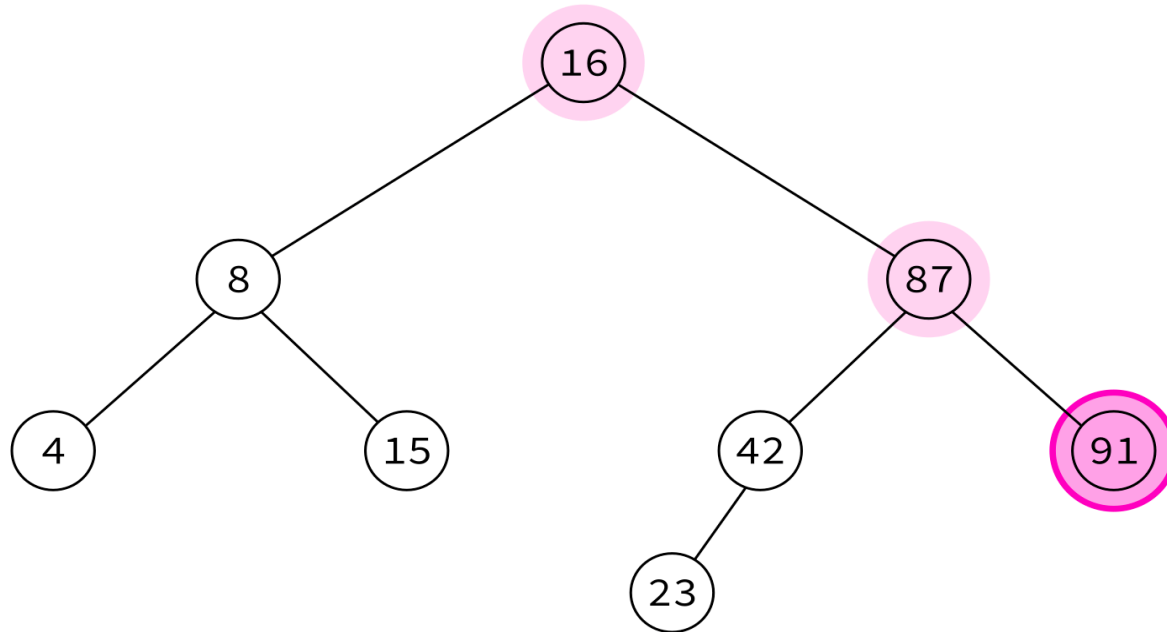
POSTORDER TRAVERSAL



4, 15, 8, 23, 42,

left, right, node

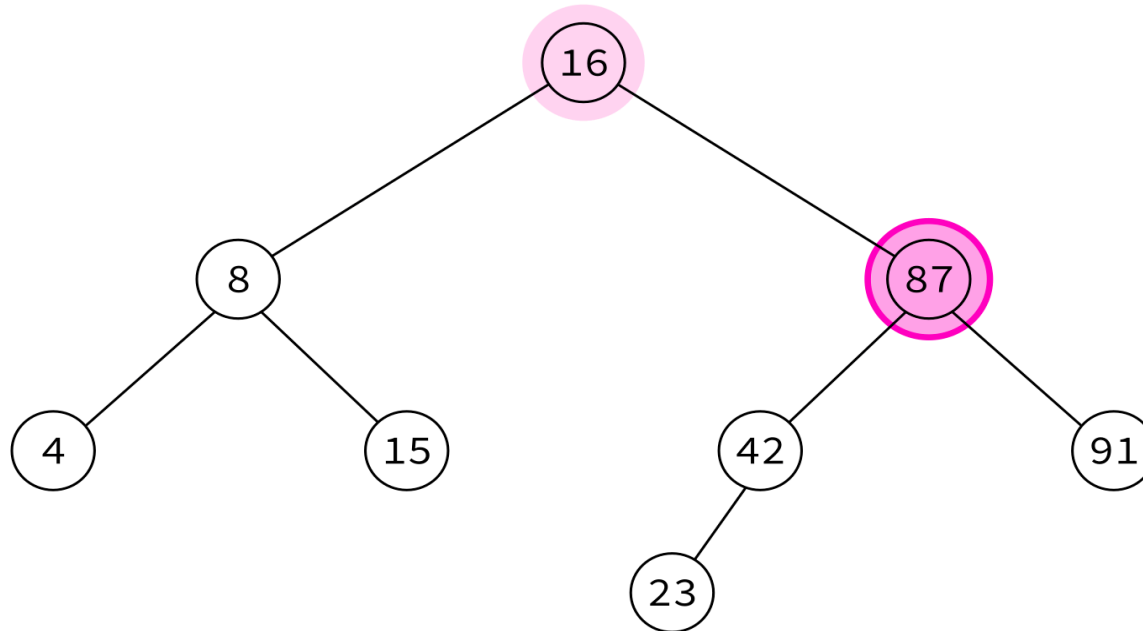
POSTORDER TRAVERSAL



4, 15, 8, 23, 42, 91,

left, right, node

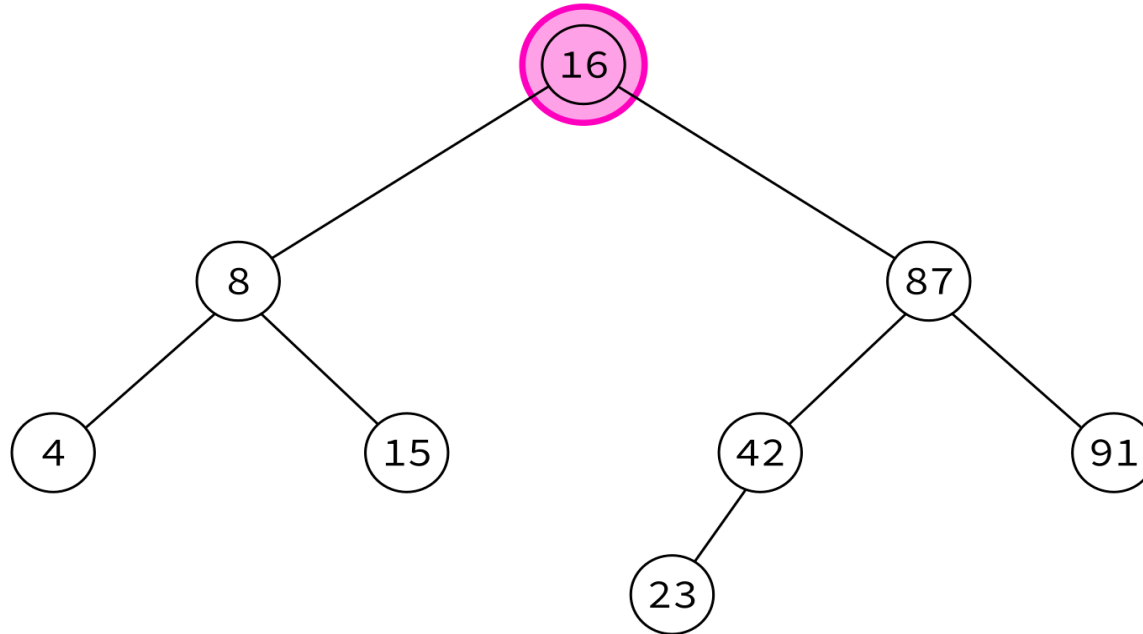
POSTORDER TRAVERSAL



4, 15, 8, 23, 42, 91, 87,

left, right, node

POSTORDER TRAVERSAL



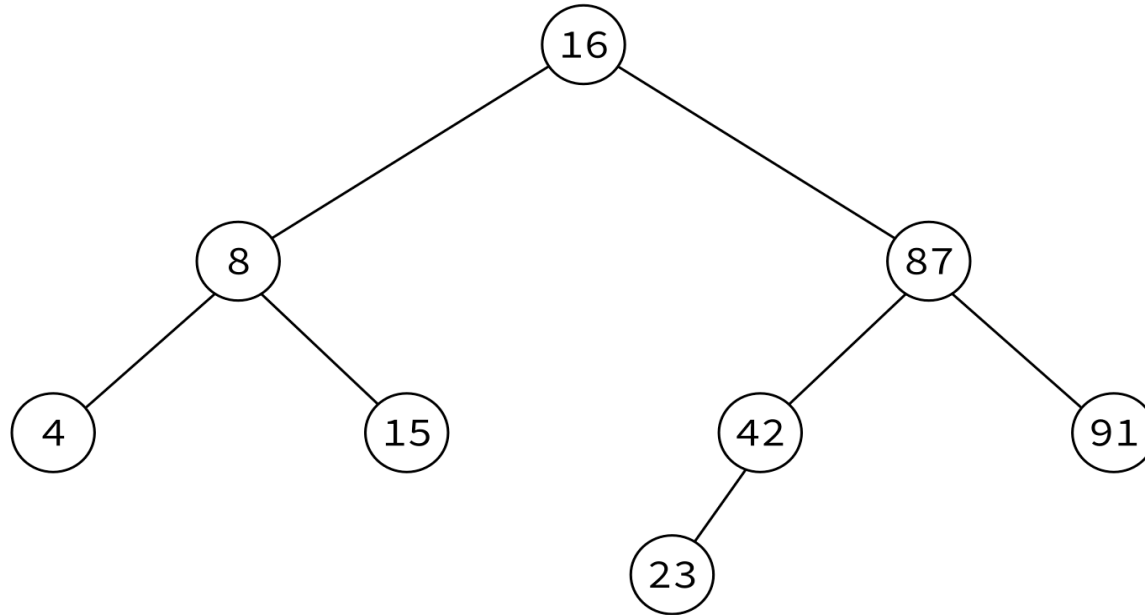
4, 15, 8, 23, 42, 91, 87, 16

left, right, node

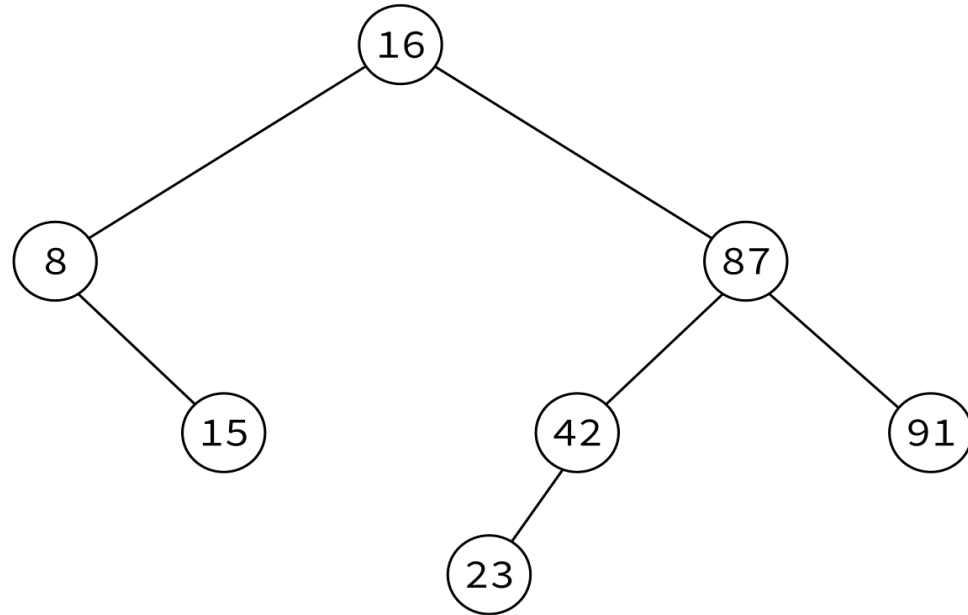
POSTORDER TRAVERSAL

Typical use: Delete the tree.

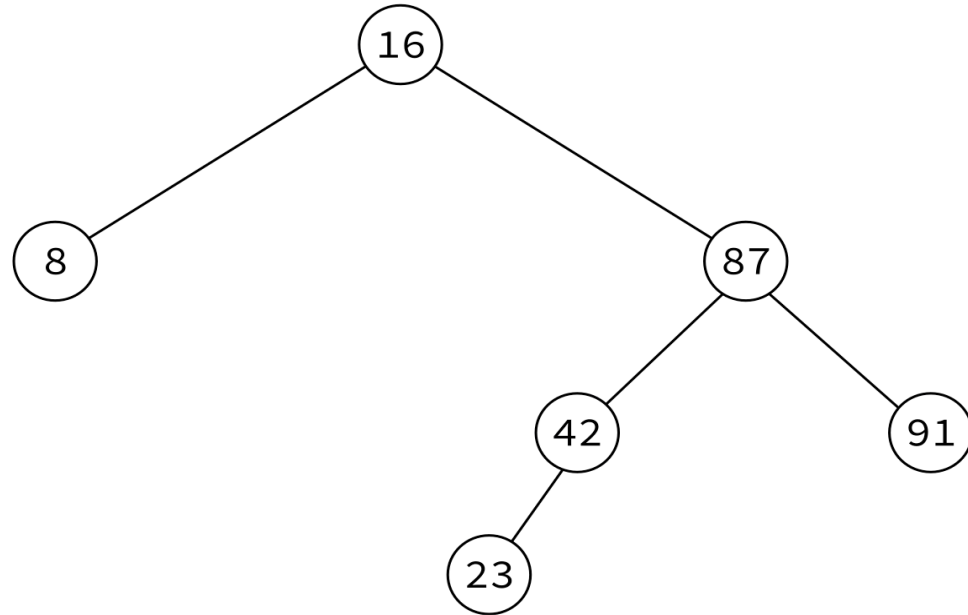
If you delete keys in postorder, then you will only ever be removing nodes without children.



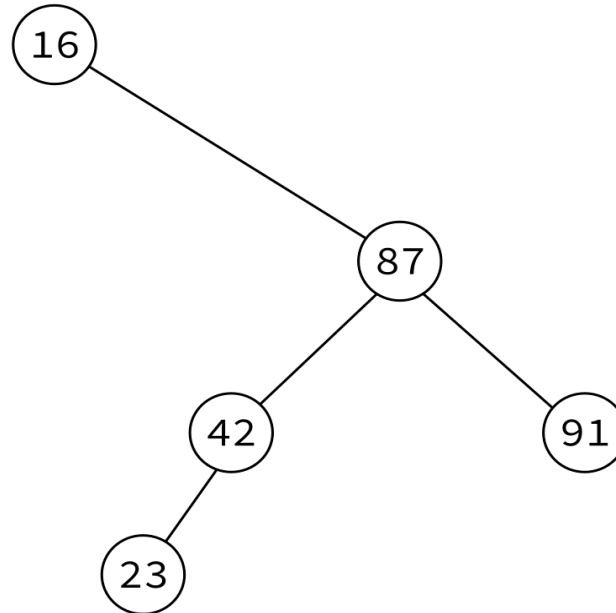
4, 15, 8, 23, 42, 91, 87, 16



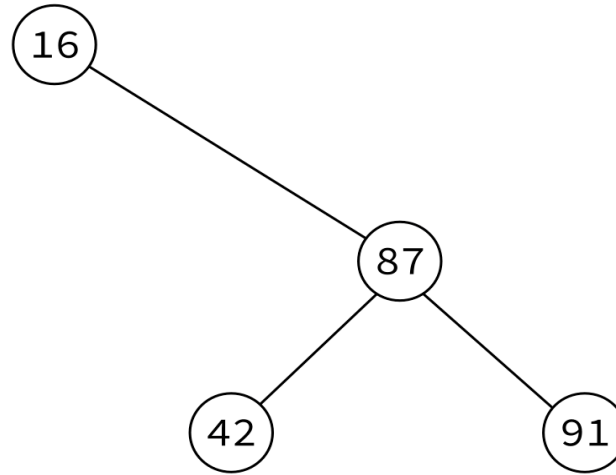
4, 15, 8, 23, 42, 91, 87, 16



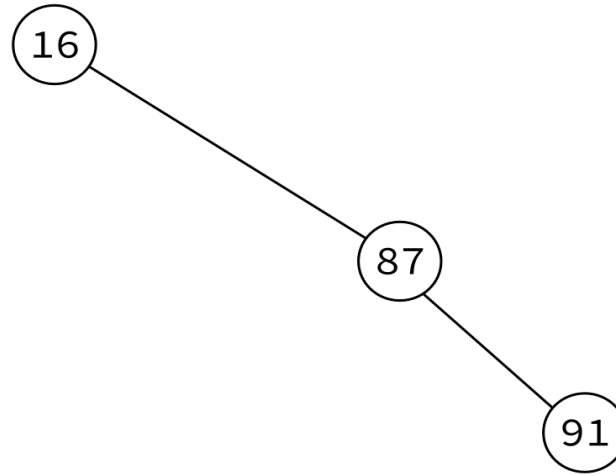
4, 15, 8, 23, 42, 91, 87, 16



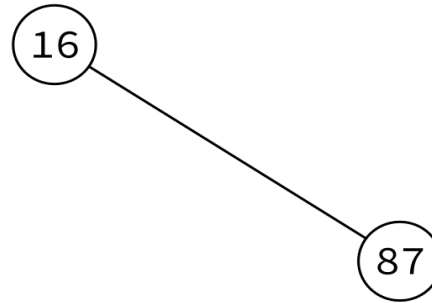
4, 15, 8, 23, 42, 91, 87, 16



4, 15, 8, 23, 42, 91, 87, 16



4, 15, 8, 23, 42, 91, 87, 16



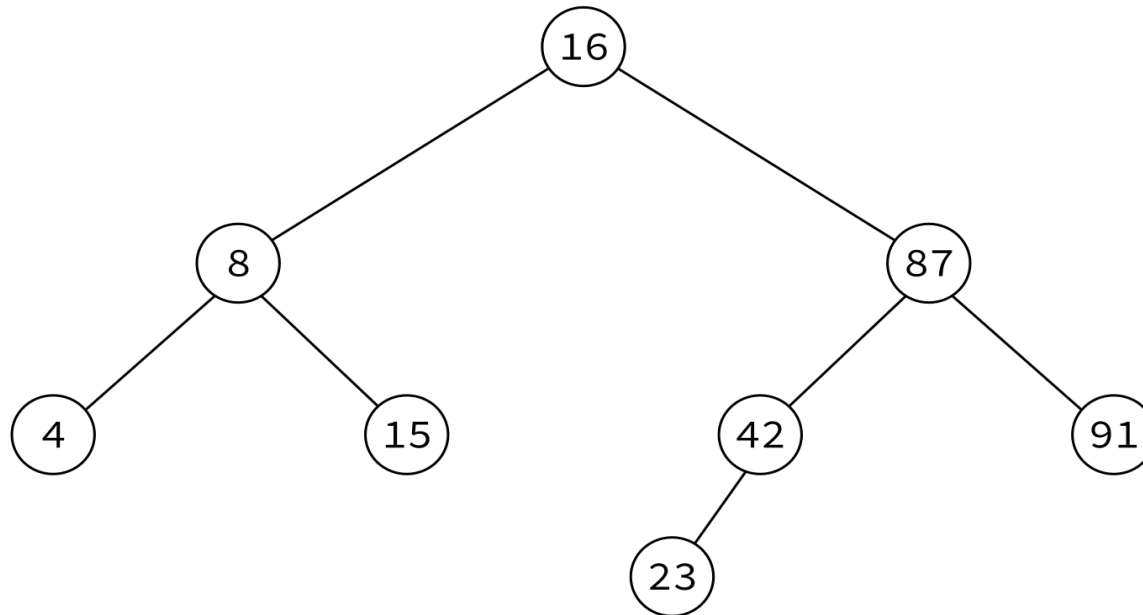
4, 15, 8, 23, 42, 91, 87, 16

16

4, 15, 8, 23, 42, 91, 87, 16

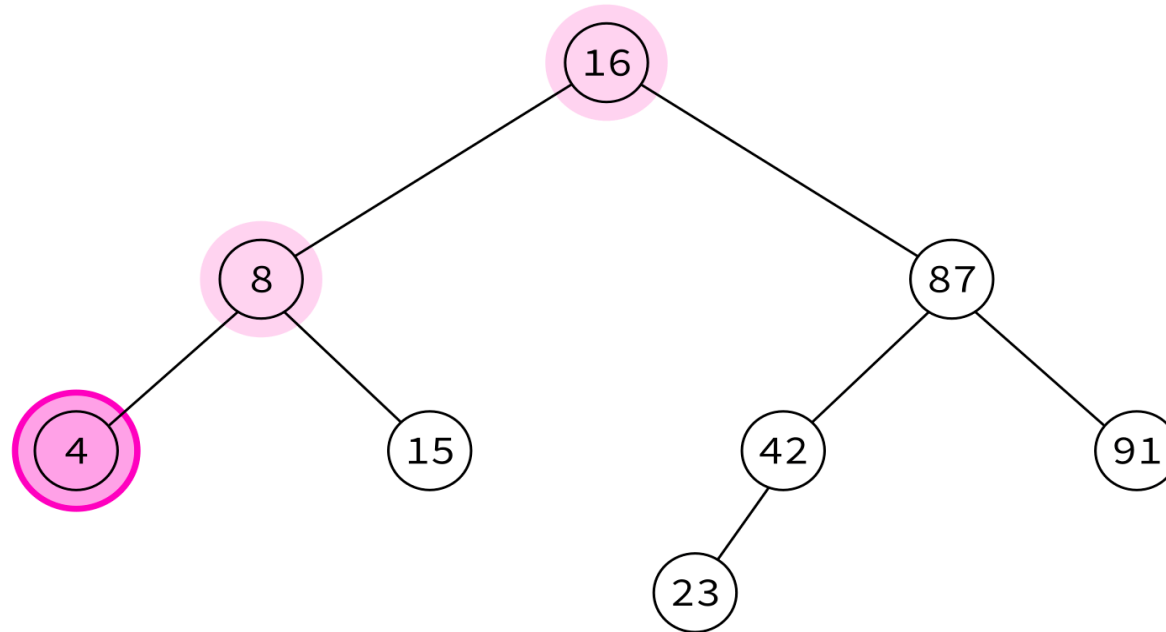
4, 15, 8, 23, 42, 91, 87, 16

INORDER TRAVERSAL



left, node, right

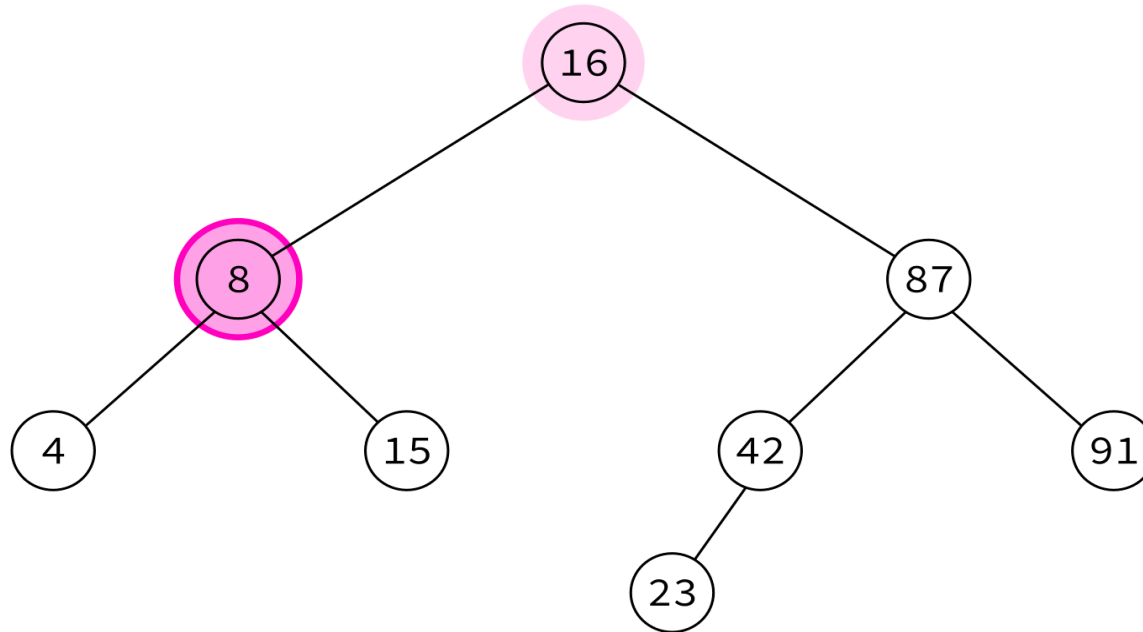
INORDER TRAVERSAL



4,

left, node, right

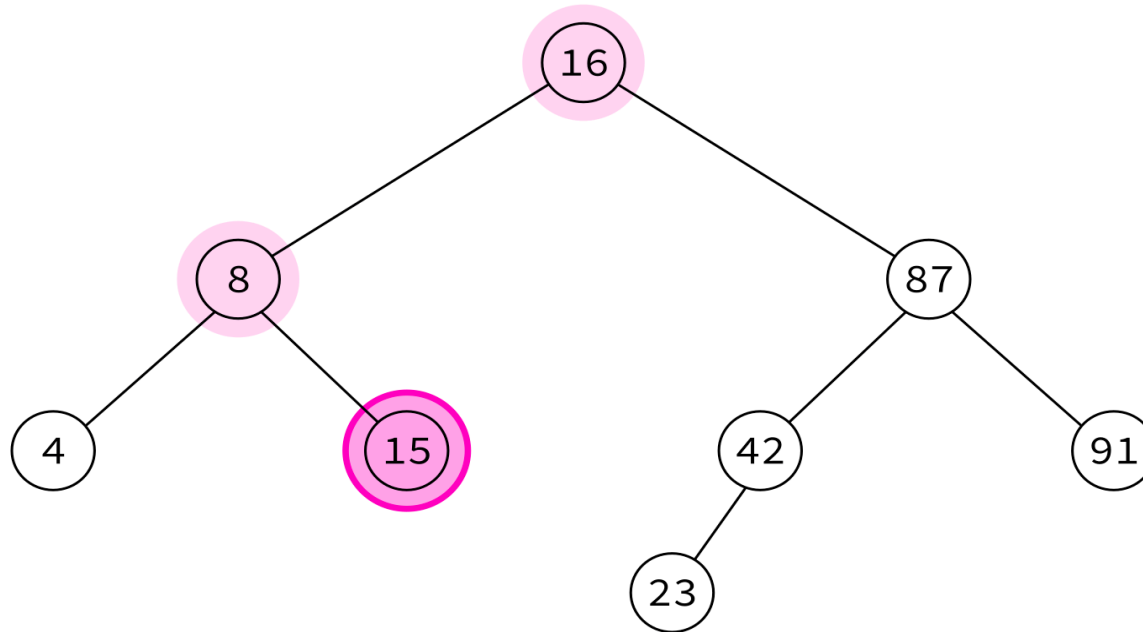
INORDER TRAVERSAL



4, 8,

left, node, right

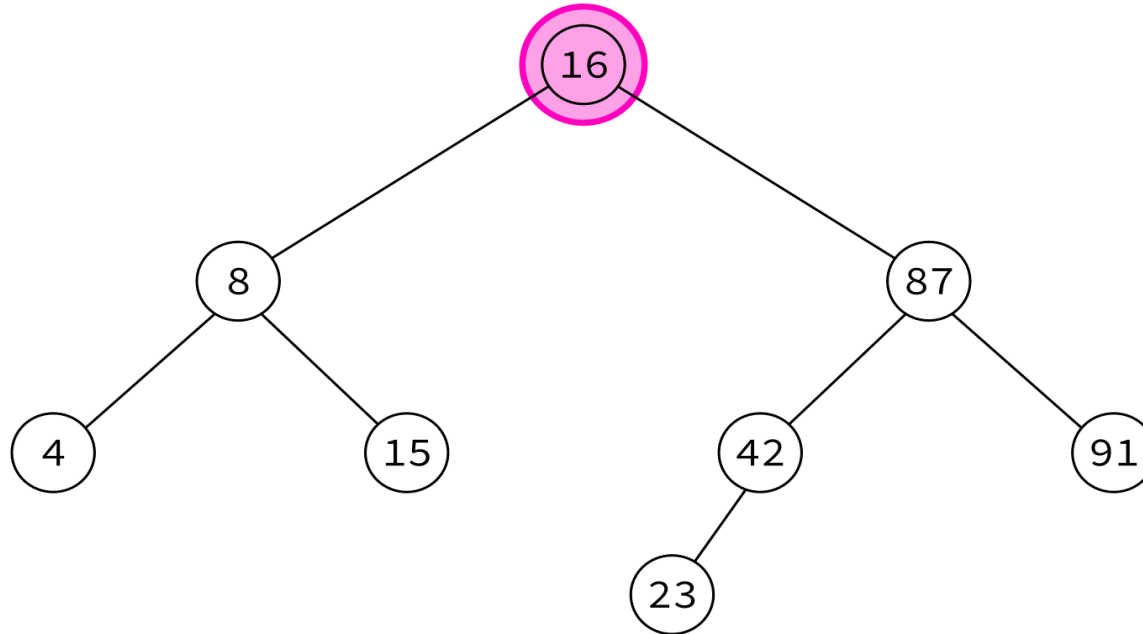
INORDER TRAVERSAL



4, 8, 15,

left, node, right

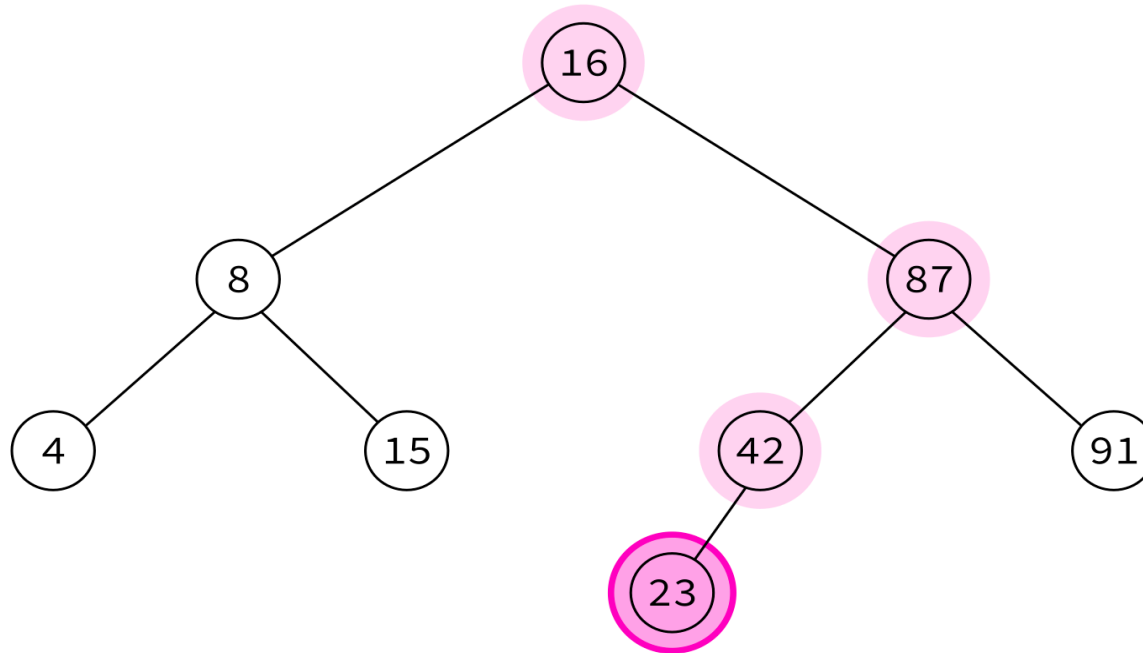
INORDER TRAVERSAL



4, 8, 15, 16,

left, node, right

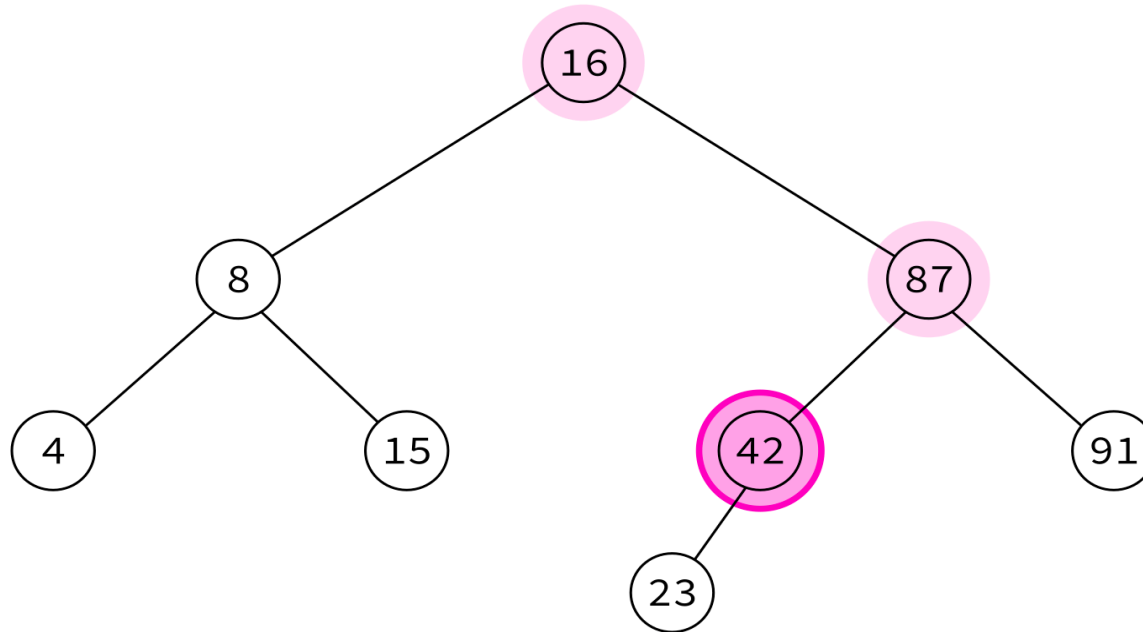
INORDER TRAVERSAL



4, 8, 15, 16, 23,

left, node, right

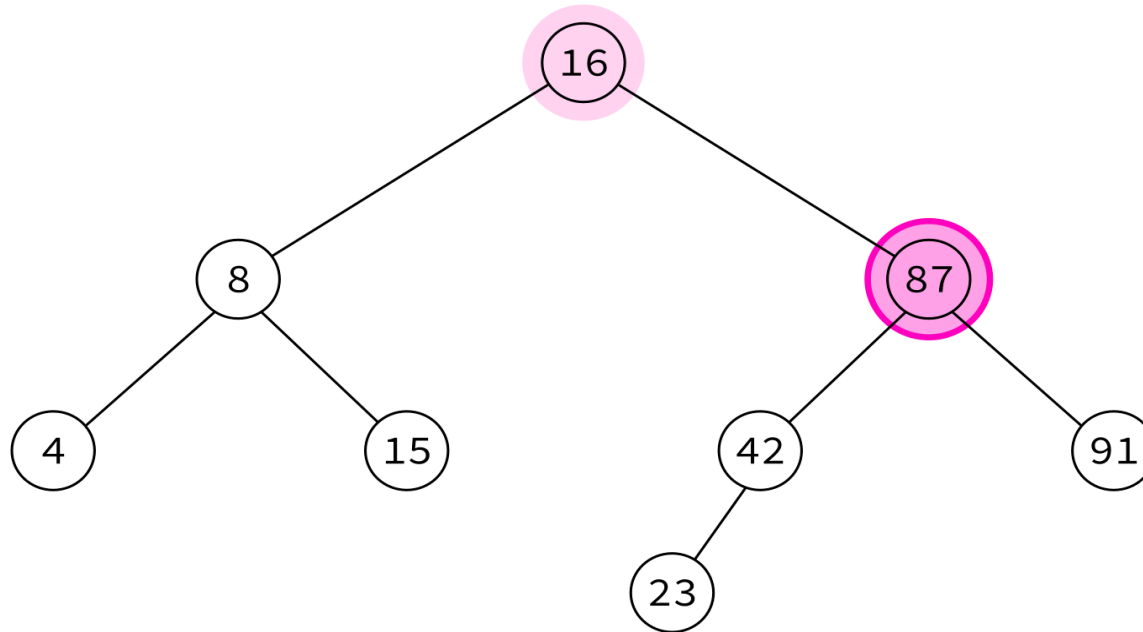
INORDER TRAVERSAL



4, 8, 15, 16, 23, 42,

left, node, right

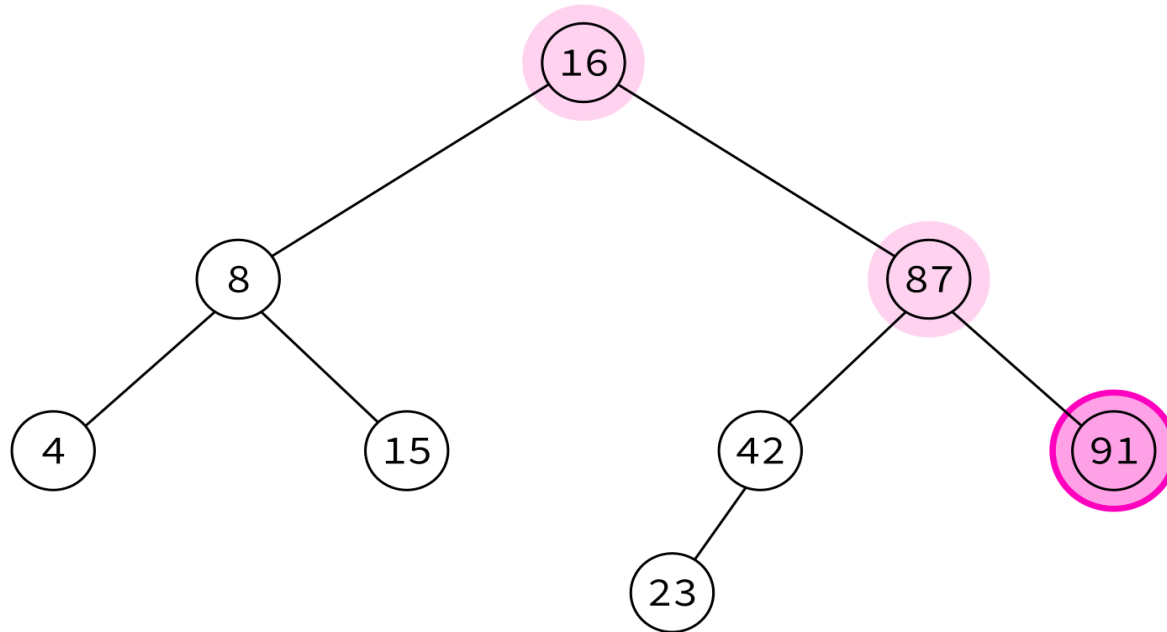
INORDER TRAVERSAL



4, 8, 15, 16, 23, 42, 87,

left, node, right

INORDER TRAVERSAL



4, 8, 15, 16, 23, 42, 87, 91

left, node, right

INORDER TRAVERSAL

Typical use: Turn a BST into a sorted list of keys.

REFERENCES

- In optional course texts:
 - [Problem Solving with Algorithms and Data Structures using Python](#) by Miller and Ranum, discusses binary trees in [Chapter 7](#).
- Elsewhere:
 - [Cormen, Leiserson, Rivest, and Stein](#) discusses graph theory and trees in Appendices B.4 and B.5, and binary search trees in Chapter 12.

REVISION HISTORY

- 2022-02-28 Initial publication

